# **Tessellations**

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"A **tessellation** is the tiling of a plane using one or more geometric shapes, called tiles, with no overlaps and no gaps".

A tessellation is **regular** if it satisfies the following conditions.

- 1. The tessellation must tile a floor (that goes on forever) with no overlapping or gaps.
- 2. The tiles must be regular polygons and all the same.
- 3. Each vertex must look the same.

#### Problem 1

- 1. Draw a regular tessellation of triangles.
- 2. Draw a regular tessellation of squares.
- 3. Can you draw a regular tessellation of pentagons?
- 4. How about hexagons?

Show that there are no other regular tessellations except triangles, squares, and hexagons.

A tessellation is **semi-regular** if is made of two or more regular polygons such that the pattern at each vertex is the same.

## Problem 3

Draw a semi-regular tessellation made of triangles and hexagons.

- 1. Draw a semi-regular tessellation made of triangles and squares.
- 2. Find all different semi-regular tessellations made of triangles and squares.

- 1. Draw a semi-regular tessellation made of a triangle, square, and hexagon.
- 2. Draw a semi-regular tessellation made of triangles and hexagons.
- 3. Find all different semi-regular tessellations that contain hexagons.

Find a semi-regular tessellation made of squares and octagons.

Find a semi-regular tessellation made of triangles and dode cagons (regular polygon of 12 sides).

Prove that there are no other semi-regular tessellations different from the ones you have found in Problem 3-7.

Following the following procedure to make your own tessellation.

- 1. Draw a square of 1 inch.
- 2. Write **NW** in the northwest corner, **SW** in the southwest corner, **NE** in the northeast corner, and **SE** in the southeast corner.
- 3. Draw a random line on the paper left-to-right.
- 4. Draw a second random line on the paper top-to-bottom.
- 5. Cut out your shapes on the lines you drew.
- 6. Put the pieces together so corners are in the middle and they spell "SE-SW-NW-NE".
- 7. Tape the pieces together.
- 8. Trace you figure with a pencil on a piece of white paper.
- 9. Extend your figure parallelly on the white paper.
- 10. Color your figure.