## POWER OF POINT RELAY

2-1 $D E$ is tangent to the circle. $D E=10$ and $F G=15$. Compute DF.


2-2 $\quad \mathrm{T}=\mathrm{TNYWR} . \quad \mathrm{UV}=3 ; \mathrm{VW}=12 ; \mathrm{UY}=\mathrm{T}$.
Compute YZ.


## 2-3 T=TNYWR

Circle P of radius 3 and circle Q of radius T intersect at A .
$P Q=6$. Compute $A B$.


## ANSWERS

2-1 $\quad \underline{\mathbf{5}}$ Use the formula: $\mathrm{PB}^{2}=\mathrm{PC} * \mathrm{PD}$
Let $x=D F . \quad D E^{2}=D F^{*} D G$ or $10^{2}=x(x+15) \quad x^{2}+15 x-100=0 \quad(x+20)(x-5)=0, x=D F=5$

2-2 4 Use the formula: $P A * P B=P C$ * PD
Let $x=Y Z . \quad U V^{*} U W=U Y^{*} U Z$ or $3^{*} 15=T(T+x) . \quad x=\left(45-T^{2}\right) / T$. Since $T=5, x=Y Z=20 / 5=4$

2-3 Let $C D=x$ and $A B=y$. Then $P C=3-x$
$P C+C Q=P Q=6$, then $(3-x)+T=6$, or $x=T-3$. Also, $P E=6+T$.
From Power of Point on $\mathrm{P}: ~ \mathrm{PA} * \mathrm{~PB}=\mathrm{PC} * \mathrm{PE}$

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3(3+y)=(3-x)(6+T)
$$

$9+3 y=(6-T)(6+T) . \quad y=\left(36-T^{2}-9\right) / 3$.


With $T=4, y=A B=(27-16) / 3=11 / 3$

## $11 / 3$

